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Enhancing Parallel Scheduling of Grid Jobs in a Multicored Environment

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Abstract: The computing Grid has emerged as a platform to solve the complex and ever-increasing processing need of man and advances in computing technology have birthed the multicore era aimed for high throughput and efficient parallel computing. However, most systems still rely on the underlying hardware for parallelism despite the hard evidence that sequential algorithms do not optimally exploit parallel systems. This research seeks to harness the benefits of multicore systems using job and machine grouping methods to enhance parallelism in the scheduling of Grid jobs. The paper presents the result of two separate experiments on a method that parallelize scheduling algorithm on two multicore platforms. An arbitrary method was employed to group machines; a summation of the total processing power of machines in each group was made. To ensure load balancing, jobs were allocated to machine groups based on the ratio of the total processing power of the machines in each group. The MinMin Grid scheduling algorithm was implemented independently within the groups using a range of threads varied in powers of two. Also, the numbers of groups were varied between 2, 4, and 8. The same experiment was executed on a single processor computer; a duocore machine and a quadcore machine. A performance improvement of 16% to 85% was recorded by the group method against the best ordinary MinMin results and an improvement of 50% to 84% was recorded by the group method against the ordinary MinMin on corresponding machines. We prove that an increase in the number of groups results in improved performance on corresponding machines (approximately 2 times using 2 groups, approximately 3 times using four groups, and approximately 6 times using 8 groups). And most importantly, we established that as the number of processors increases, the grouping method makes more significant improvements over the ordinary MinMin scheduling algorithm executed on the multicore systems.

Keywords: Multicore-environment, Parallelism, Multi-scheduling, Machine Grouping, Job Grouping, Scheduling

1. Introduction

The advent of Grid computing has been acclaimed as the paradigm to solve the ever-increasing computing need of an ever-demanding world while multicore systems have been heralded as the major architecture choice for modern computing platforms - this is anticipated to remain so for long [1, 2] and [3]. However, it has been shown that sequential algorithms do not gain much from parallel systems if the algorithm is not Parallelized [4]. Current Grid scheduling algorithms are mostly sequential and do not exploit the inherent benefits in the underlying multicore systems, while most others focus on scheduling parallel jobs rather than scheduling jobs in parallel. Scheduling of Grid jobs without exploiting the underlying multicore hardware in this era of multicore systems poses a negative trend for the growth and purpose of the Grid. The method presented in this work provides a general means of Parallelization of sequential algorithms. The method uses several independent groups to enable several scheduling instances within the group (multi-scheduling), this greatly enhances parallelism.

The remainder of the paper is organized as follows: the next section discusses related literature. Section 3 discusses the proposed method and presents results and analysis. Section 4 makes recommendation and section 5 discusses conclusion and future thoughts.

2. Related Work

The NP-completeness of heterogeneous systems requires heuristics to ease the problem-solving. Exploiting a method that enhances the efficiency of multicore systems for the overall benefit of grid scheduling will be beneficial to the growth of the Grid. Advances in computer hardware technology are aimed at parallelizing processing, high throughput, performance improvement, speedup, and efficiency [5]. However, most Grid scheduling algorithms remain sequential; such algorithms 'eat up' the gains in hardware technology', impede performance, and do not guarantee maximum speedup [6, 7] and [4]. The multicore era, therefore, requires a parallel approach to programming [8-10]. However, parallelizing sequential algorithms are quite complex and not completely guaranteed. Therefore, a method that enhances parallelism in the execution of all algorithms is sought; grouping jobs and machines before simultaneously scheduling independent groups (multischeduling) enhances parallelism on the multicore systems and increases throughput [11].

This work uses job and machine groups to exploit parallelism on multicore systems.

2.1. Parallelism and Multicores

Serial computing is replete with drawbacks [12], multicore technology was, therefore. the direction for future computing interest [13] and [14]. However, major advances in computing technology come with a paradigm shift in programming [15]; based on calls by many researchers to embrace parallelism; a better programming method that enhances the performance of multicore systems should therefore be of interest to researchers because the potentials of multicore systems are largely being under-utilized on current systems [7, 16, 17].

In this regard, several researchers have experimented with the execution of algorithms on parallel systems: an experiment was conducted on clusters of CPU-GPU to speed up queries from high dimensional holistic data that are being updated constantly, the experiment attained efficiency in handling queries in [18]. A method that exploited parallel algorithms to scale multicore systems and obtained optimal results was presented in [19].

A method that used a code transformation to create data parallelism latent in parallel applications to enhance resource utilization and speedup on chips to facilitate parallelism on the hardware was exploited in [20]. While a method that efficiently executed (Precedence-constrained Task Graphs) PTGs on a distributed system with heterogeneous processing elements connected through a set of shared heterogeneous buses was proposed in [21].

A novel framework that automatically, efficiently, and recursively computes the divide and conquer algorithms for a set of dynamic programming problems in multicore systems was exploited in [22]. In the same vein, optimization in energy consumption and improvement in schedule length was achieved by employing a parallelizing scheduling method to find a solution to the duplication-based scheduling problem in [23]. Also, an experiment on parallel programming paradigms like OpenMP on CPU cluster and CUDA on GPU cluster using (Breadth-First Search) BFS and (Depth-First Search) DFS graph algorithm that attained a speedup of 187 to 240 by CUDA on GPU over the OpenMP on CPU clusters was executed in [24]. They however noted that the CPU clusters underperformed due to communication overheads and idle time.

The gains of parallel computing systems have been exploited by researchers in other fields as well: In bioinformatics; parallel programming technology was employed for genome sequence processing in [25]. In electronics, a parallel computation method to curb the bottleneck incurred by serial computation of CRC was exploited in [26]. The method efficiently increased speed-up in the computation of (cyclic redundancy check) CRC computation on CPU and Field Programmable Gate Array (FPGA). And in geospatial statistics; parallelism was exploited on a parallel hardware architecture in the computation of environmental data in [27] and [28].

Though these researches all aimed at attaining throughput, speed-up, and optimize processing on parallel architecture; no special method was employed to enhance parallelism. However, optimal exploitation of parallel architecture requires a fundamental approach to the way programming is done [29, 30, 8, 10, 7]. This requirement necessitated the group-based approach undertaken in this work.

2.2. Grouping of Jobs Before Scheduling

Grouping of jobs before scheduling has been used extensively by researchers to achieve different aims. A method that grouped fine-grained jobs to form coarse-grained jobs before scheduling to improve response time was exploited in [31]. A method that grouped jobs before transmitting to Grid resources for computation was exploited in [32]. While another method that exploited grouping to reduce the (communication computation ratio) CCR before the schedule was presented in [33]. Also, a method that divides the base relation into several independent sub-cubes to reduced exponentiality and efficiently performed queries was exploited [18] – here, the sub-cubes are likened to groups.

In these works; parallelism dependent on the underlying hardware; the group was used to attain optimality or efficiency but not really in aiding parallelism.

This research employs grouping as platforms to parallelize the scheduling of grid jobs on multicore systems. The groups enable the threads to execute independently in multi-scheduling of jobs within the groups - taking advantage of the multicores.

In line with this research, significant improvement was achieved in [11] using job and machine groups before scheduling. However, the effect of increasing the number of groups could not be investigated further. As a result, a dynamic means of grouping grid jobs and grid machines for efficient multi-scheduling was proposed in [34]. The method recorded significant improvement with increasing groups.

Hence, various strategies to group machines and Grid jobs before scheduling on an HPC system were experimented with in [35] and significant improvement was recorded by all methods as the number of groups increases. However, on the HPC system, the number of CPUs is constant and the effect of varying the number of processors on the grouping method was recommended for investigation. A random machine grouping method and size-proportional-to-speed method of job grouping were proposed in [36] and a performance improvement of 16% to 71% on a duocore machine was achieved. The researchers noted that investigating further on a system with more cores was necessary to know the effect on the method. So, the same work was extended on a quadcore system in [37] and an improvement of 50% to 86%. However, the trend of improvement on both platforms needed to be examined. This paper combines the results and added more analysis of the separate experiments carried out in [36] and [37].

3. Parallel Scheduling of Grid Jobs in a 'Multicored' Environment

This research aims at exploring the parallelism inherent in multicore systems by using a method of job and machine grouping. An arbitrary method was employed to group machines; a summation of the total processing power of machines in each group was made. To achieve load balancing, jobs were then allocated to the machine groups based on the ratio of the total processing power of the machines in each group.

A range of one to eight threads in powers of two (1 to 8 step $2^n\ n \in [0,1,2,3]$) was used in varied experiments. Also, the number of groups was varied between 2, 4 and 8. The experiment was executed on a single processor system, a duocore system and a quadcore system.

The MinMin algorithm [38] was chosen as a benchmark in this work because it has been adopted by several other researchers for benchmarking [39-48].

3.1. Job and Machine Grouping

The algorithms for grouping jobs and machines used in this experiment have been presented in [36, 37].

3.2. Experimental Design

This work is based on the series of experiments carried out in [36] and [37].

3.3. Results and Data Analysis

This section discusses results from all the experiments from the two previous works referred in section 3. In the discussion, 1Thrds, 2Thrds, 4Thrds or 8Thrds refer to the number of threads used in the experiment. SingleCPU or SingleProc, 1CPU or 1Proc refer to result obtained on the single processor machine; duocore refers to results from the duocore machine while Quadcore refers to results obtained on the quadcore machine. Also, 2Grp, refers to two groups, 4Grp refers to four groups and 8Grp refers to eight groups. The proposed method Size-Proportional-to-Speed and random method abbreviated as SpdRnd. A combination of group numbers, number of threads, and machines are used to refer to a specific result. For instance, 4ThrdsDuocore4Grps represent results obtained using 4 threads and 4 groups on the duocore machine.

3.4. Performance of the MinMin Algorithm on the Three Computing Platforms

This section discusses the result of the ordinary MinMin (MinMin without the group method). Table 1 shows the results and performance of the ordinary MinMin on the three different computer platforms (single processor machine, duocore machine, and quadcore machine) and the computed performance improvements. The Single processor system took a total of 1235755 ms to schedule the range of jobs. The duocore system used a total of 220726 ms to schedule the range of jobs while the quadcore machine used 136818ms to schedule the same range of jobs (from 1000 to 10,000 step 1000).

Using the ordinary MinMin, there was a performance improvement of 5.6 times or 82% by the Duocore machine over the Single processor machine. The quadcore machine improved performance 9 Times or 88% over the single processor machine. And the Quadcore machine improved performance 1.6 times or 38% over the duocore machine.

These results show that the MinMin algorithm is scalable and gained immensely from the multicore system's underlying parallelism. However, the question is are these improvements recorded by the MinMin on the duocore and quadcore machines enough not to try a different method that enhances parallelism on the multicore systems? Analysis of results in sections 3.5, 3.6, and 3.7 between the performance of the MinMin and the group method on the multicore systems will provide answers.

Table 1. Scheduling result of MinMin algorithm on the three machines.

Jobs Limit	MinMin2Thrds (SingleCPU)	MinMin2Thrds (DuoCore)	MinMin4Thrds (QuadCore)
1000	4500	690	399
2000	17672	2800	1795
3000	40250	6410	4222
4000	66922	10674	7188
5000	90407	26432	9994
6000	116922	19275	12700
7000	154781	24914	16690
8000	196768	32446	21719

Jobs Limit	MinMin2Thrds (SingleCPU)	MinMin2Thrds (DuoCore)	MinMin4Thrds (QuadCore)
9000	244679	44057	27989
10000	302854	53028	34122
Total	1235755	220726	136818
Average	123575.5	22072.6	13681.8
Improvement over Single processor system (X)		5.60	9.03
Improvement over Single processor system (%)		82.14	88.93
Improvement over Duocore system (X)			1.61
Improvement over Duocore system (%)			38.015

3.5. Analysis of Results on Corresponding Machines

This section compares the result between the MinMin and the group method on corresponding machines.

Table 2 shows the results, computed total, Average, and performance improvement in multiples (X) and percentage (%) between the MinMin and the group methods on corresponding machines. This is also shown in Figure 1 while Figure 2 shows the improvement by the group method over the MinMin on the single processor machine, duocore machine, and the quadcore machine.
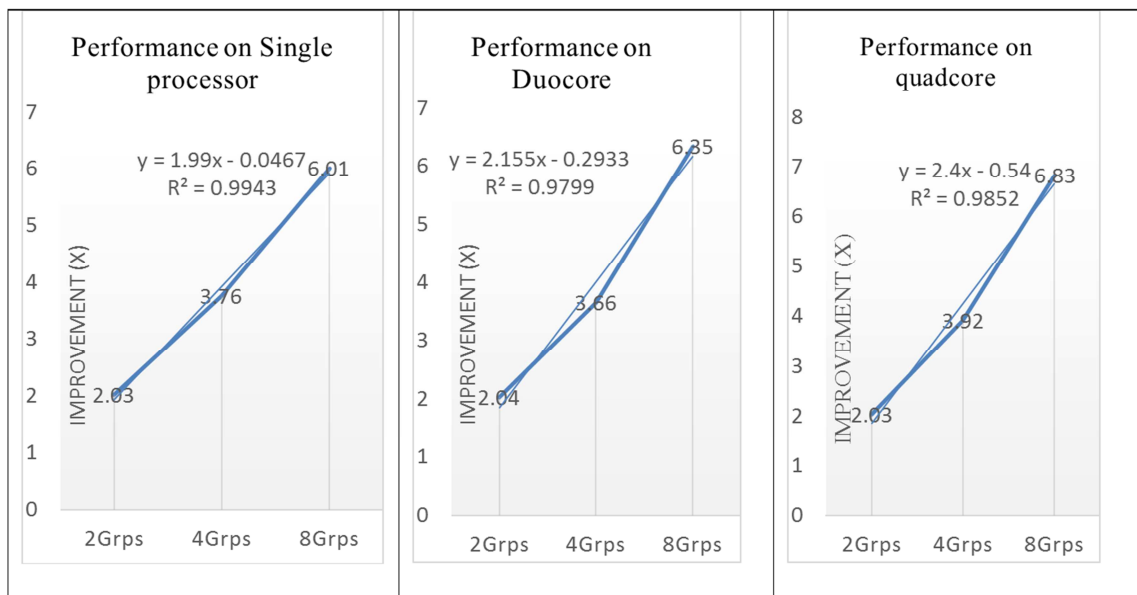

Figure 1. Performance improvement by group method on corresponding machines.
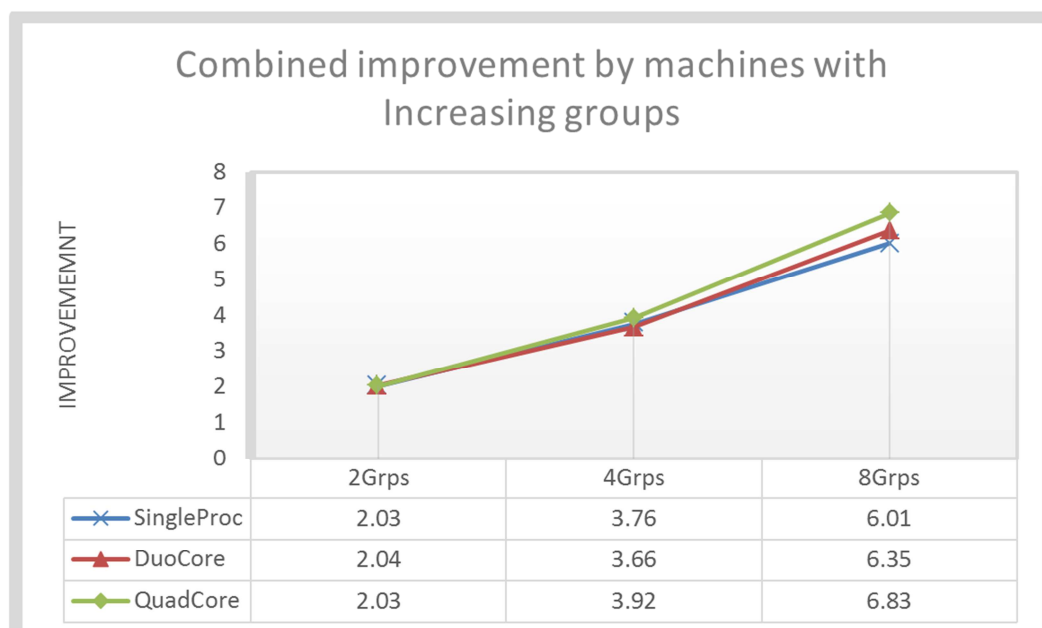

Figure 2. Combined performance improvement by group method on corresponding machines.

On the single processor machine, the group method performed 2.03 times, 3.76 times, and 6.01 times better than the MinMin when executed with 2, 4, and 8 groups respectively. This represents 50%, 73%, and 83%. This result and computed improvement indicate that the group method performed better than the ordinary MinMin even on the single processor system.

The linear trendline on the improvement yielded the equation $Y = 1.99x – 0.0467$ and the R-Squared value of the trendline is 0.9943.

On the duocore machine, the performance was 2.04 times, 3.66 times and 6.35 times better than the MinMin which represents 50%, 72% and 84% when executed with 2, 4 and 8 groups respectively. The linear equation on the duocore performance trendline $Y = 2.155x – 0.2933$ with the R-squared value of 0.9799.

On the quadcore machine, the group method performed 2.03 times, 3.92 times and 6.88 times better than the MinMin algorithm. This represents 50%, 74% and 85% when executed with 2, 4 and 8 groups respectively. The trendline on the improvement yielded equation $Y = 2.4x – 0.54$ and the

R-Squared value of the trendline is 0.9852.

The correlation of results and improvements between the group method and MinMin on corresponding machines is (0.99) which indicates that the group methods results are strongly reliable and acceptable.

The linear equations indicate that performance improvement Y depends on the number of groups (x) and increases with an increase in the number of groups. While the R-Squared value of 0.9x on the trendlines indicates a good fit, it also indicates the reliability and repeatability of the results.

Even though the MinMin is also scalable, the result indicates that the group method improves the performance of the parallel architectures (multicore systems) by an approximate factor of 2 when using two groups, an approximate factor of 3 when using four groups and an approximate factor of 6 when using 8 groups.

Figure 2 and the linear equations generated from the improvement trendline from the three computing platforms indicate that there is a general performance improvement with increasing cores.

Table 2. *Analysis of corresponding results and performance.*

	Single Processor				Duocore				Quadcore			
	MinMin	2Grps	4Grps	8Grps	MinMin	2Grps	4Grps	8Grps	MinMin	2Grps	4Grps	8Grps
1000	4500	2360	1094	594	690	375	319	95	403	189	111	78
2000	17672	7907	3876	2031	2800	1360	617	331	1775	759	337	196
3000	40250	17031	9063	4360	6410	2628	1334	609	4203	1543	648	396
4000	66922	28468	13656	9359	10674	4665	2138	1575	7431	2570	1297	671
5000	90407	40453	22672	12985	26432	7680	3832	2323	9903	4339	1928	1178
6000	116922	59781	32578	19062	19275	9607	5481	2927	12984	6433	3089	1568
7000	154781	79499	42047	26234	24914	14322	7888	4864	16872	9079	4315	2361
8000	196768	94781	54172	34453	32446	17156	9967	5672	21956	11261	5758	2855
9000	244679	119609	67438	41250	44057	22976	12796	7273	27778	14340	7082	4506
10000	302854	157970	82423	55282	53028	27406	15921	9080	34570	17385	10593	6379
Total	1235755	607859	329019	205610	220726	108175	60293	34749	137875	67898	35158	20188
Avg	123576	60785.9	32902	20561	22073	10817.5	6029	3474.9	13787.5	6789.8	3515.8	2018.8
Improvement (X)	(X)	2.03	3.7	6.01	(X)	2.04	3.66	6.35	(X)	2.03	3.92	6.83
Improvement (%)	(%)	50	73	83	(%)	50	72	84	(%)	50	74	85

3.6. Comparison of Result on the Three Computing Platforms Against the Best MinMin Result

This section compares the best ordinary MinMin result (obtained on the quadcore) against the group method result from other platforms. On the three computing platforms, the ordinary MinMin result from the quadcore machine was the best. Hence, the ordinary MinMin result yielded by execution on the quadcore system was used.

Table 3 shows the result and computed total scheduling time of the ordinary MinMin algorithm executed on the quadcore compared against results of the group method from the three platforms. It also shows the computed total and average time used in scheduling the range of jobs. While Table 4 and Table 5 shows the computed performance improvement between the machines in multiples (X) and in percentage (%) respectively.

From Table 4 and Table 5, the MinMin algorithm executed on a quadcore system performed better than the group method executed on the single processor system by 4.40

times, 2.37 times and 1.51 times (or 77%, 57% and 33%) when using two, four and eight groups respectively. This is shown in the first part of Figure 3 labeled A to B (and Figure 4 labeled Single processor). As the number of groups increases, it can be seen that the graph was falling from left to right – this indicates that the group method was able to increase performance as the number of groups increases – though not enough to match the performance improvement of the MinMin on the quadcore machine.

This result indicates that the MinMin algorithm is scalable and benefitted from parallelism on the quadcore while the group method executed on the single processor system underperformed due to the absence of parallelism which the method requires but could not be supported by the single processor system. The group method targets multicore systems, so it is not suited for single processor systems.

The second part of the graph in Figure 3 and Figure 4 (labelled C to D or duocore) shows the performance of the duocore system using the group method over the ordinary MinMin executed on the quadcore. The group method on the

duocore performed better than the MinMin by 1.21 times, 2.04 times and 3.56 times (or 16%, 49% and 71%) when using two, four and eight groups respectively for scheduling. This caused the aggregate graph to rise at a point beginning from duocore 2 groups and continued to rise to duocore 8 groups.

The group method exploited the parallelism inherent on the Duocore system and this resulted in the improved performance over the ordinary MinMin algorithm executed on quadcore.

Points E to F in Figure 3 (shown as quadcore in Figure 4) shows the performance of the quadcore system over the ordinary MinMin as the group increases from 2 to 8 groups. The quadcore machine recorded performance improvement of 2.03 times, 3.98 times and 7.10 times (or 50%, 74% and 85%) over the MinMin when using 2, 4 and 8 groups respectively.

This analysis indicates that performance improvement is attained both by an increase in the number of groups and an increase in the number of cores.
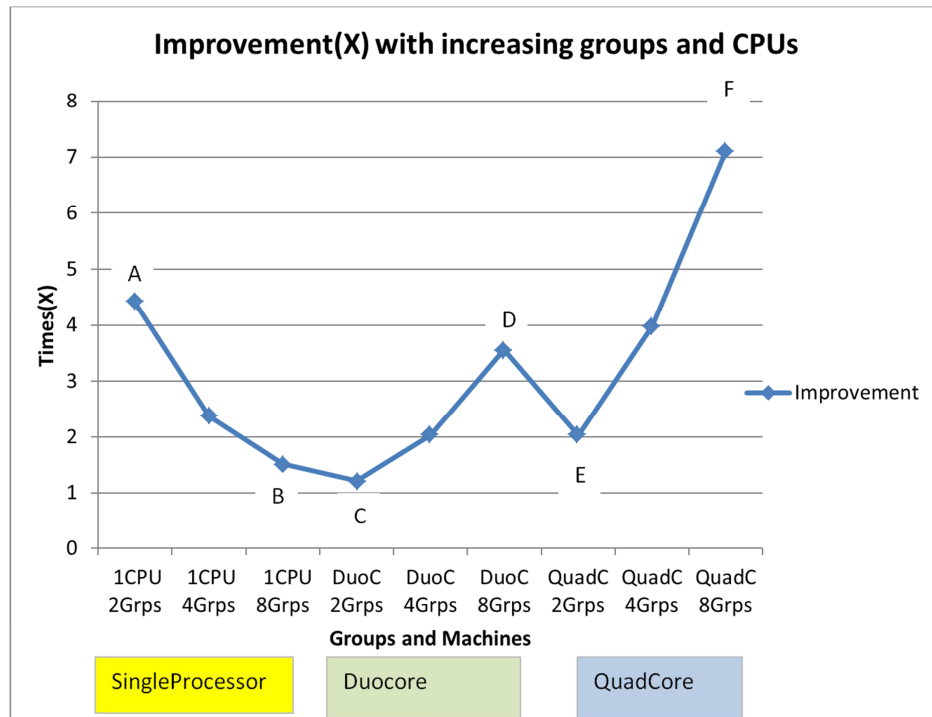

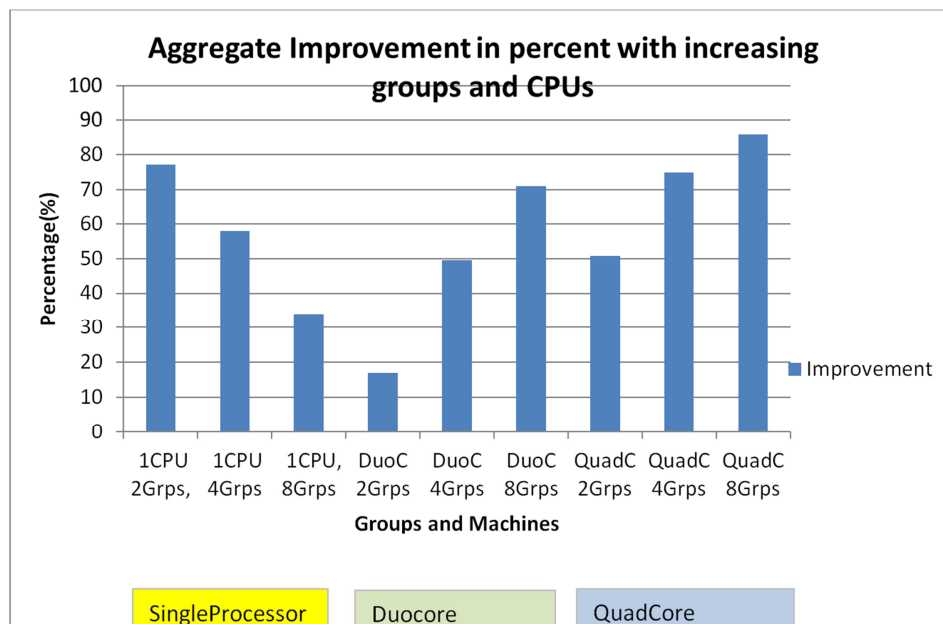**Figure 3.** *Performance trend among between the systems.*

Figure 4. *Aggregate performance.*

Table 3. *Experiment results from three computing platforms.*

No of Jobs	Quadcore	Single Processor			Duocore			Quadcore		
	MinMin	2Grps	4Grps	8Grps	2Grps	4Grps	8Grps	2Grps	4Grps	8Grps
1000	403	2360	1094	594	375	319	95	189	111	78
2000	1775	7907	3876	2031	1360	617	331	759	337	196
3000	4203	17031	9063	4360	2628	1334	609	1543	648	396
4000	7431	28468	13656	9359	4665	2138	1575	2570	1297	671
5000	9903	40453	22672	12985	7680	3832	2323	4339	1928	1178
6000	12984	59781	32578	19062	9607	5481	2927	6433	3089	1568
7000	16872	79499	42047	26234	14322	7888	4864	9079	4315	2361
8000	21956	94781	54172	34453	17156	9967	5672	11261	5758	2855
9000	27778	119609	67438	41250	22976	12796	7273	14340	7082	4506
10000	34570	157970	82423	55282	27406	15921	9080	17385	10593	6379
Total	137875	607859	329019	205610	108175	60293	34749	67898	35158	20188
Avg	13787.5	60785.9	32901.9	20561	10817.5	6029.3	3474.9	6789.8	3515.8	2018.8

Table 4. *Combined Improvement Analysis in Multiples (X).*

Combined Improvement Analysis in Multiples									
	Single Processor			Duocore			Quadcore		
	2Grps	4Grps	8Grps	2Grps	4Grps	8Grps	2Grps	4Grps	8Grps
1 Threads	4.37	2.36	1.53	1.29	2.22	3.95	2.03	4.07	6.96
2 Threads	4.41	2.39	1.49	1.27	2.29	3.97	2.03	3.92	6.83
4 Threads	4.43	2.38	1.52	1.07	1.61	2.76	2.03	3.96	7.52
Aggreg. Improvement	4.40	2.37	1.51	1.21	2.04	3.56	2.03	3.98	7.10

Table 5. *Combined Improvement Analysis in percentage (%).*

Combined Improvement Analysis in Percentage									
	Single Processor			Duocore			Quadcore		
	2Grps	4Grps	8Grps	2Grps	4Grps	8Grps	2Grps	4Grps	8Grps
1 Threads	77.13	57.56	34.80	22.26	54.87	74.69	50.82	75.42	85.64
2 Threads	77.32	58.10	32.94	21.54	56.27	74.80	50.75	74.50	85.36
4 Threads	77.44	57.93	34.10	6.87	37.76	63.78	50.83	74.73	86.70
Aggregate Improvement	77.30	57.86	33.95	16.89	49.64	71.09	50.80	74.88	85.90

3.7. General Discussion on the Results

The experiments were conducted on a different set of computer systems running on CPUs from a different family with different internal architecture, different clock speeds, different memory access patterns, different cache coherence, different levels of hit rate. As a result, the overall result cannot be normalized due to differences in factors that determine the performance of a computer's processor. However, the results and measured performance improvement were strongly correlated (0.99), also, the R-Squared value of the performance improvement on each machine was high (0.9x), thus indicating a high degree of correctness and reliability.

From the analysis, we demonstrated that by placing machines and independent jobs into groups before simultaneously multischeduling in parallel enhances the overall scheduling time. We find that with increased groups, the performance of the grouping method continues to improve against the ordinary MinMin on the multicore systems. We also find that there was a general increase in performance as the number of cores increases.

Relying on the underlying multicore system for parallelism is not the best for scheduling and processing - especially when the algorithm is sequential. However, our findings showed that the ordinary MinMin algorithm is scalable and performed better on the quadcore machine, then on the duocore machine and least on the single processor machine. Also, the MinMin on the quadcore performed better than the group method executed on a single processor system. This is because the MinMin algorithm scaled up on the quadcore machine while the single processor system offered but minimal parallelism for threads execution required by the group method.

On the multicore machines, the group method performed far better than the ordinary MinMin correspondingly and also when measured against the best MinMin result obtained from the quadcore. Although all the machines are not timed at the same speed, we can conclude from the analysis that the group method increases parallelism which resulted in improved performance as the number of groups increases and also as the number of cores increases.

The results and improvement analysis were highly correlated (0.99) and a plot of performance improvement on corresponding machines yielded a linear trend with increasing function and also with a high R-Squared value of 0.99. This high R-Squared value indicates a very good fit. It also indicates the reliability and predictability of the method. Generally, it shows that using more groups will continue to improve the performance of scheduling algorithms on multicore systems and also that machines with more cores will guarantee better performance over machines with fewer cores.

4. Recommendations

Results and analysis have shown that serial algorithms do not fully exploit parallelism on multicore systems. It has also been shown that serial algorithms are not completely parallelizable, for the grid to attain its goals, efforts aimed at scaling the scheduling and processing of Grid jobs in line with the ready benefits of the multicore systems should be encouraged.

The result and analysis from this experiment indicate that grouping jobs and machines before scheduling greatly enhances improvement on multicore systems. Therefore, we recommend that performance improvement methods like the group method be integrated into job scheduling and processing in the Grid.

5. Conclusion

This work combined the experiments in our previous work using the group method on three different computing platforms. The aim is to enhance the scheduling of Grid jobs by exploiting parallelism on multicore systems. On the single processor, the group method recorded 50%, 73% and 83%. Or 2.03, 3.76, and 6.01 Times improvement over the MinMin when executed with 2, 4 and 8 groups respectively.

On the duocore machine, the group method performed 50%, 72% and 84% or 2.04, 3.66, and 6.35 Times better than the MinMin when executed with 2, 4 and 8 groups respectively.

On the quadcore, the group method performed 50%, 74% and 85% or 2.03, 3.92, and 6.88 Times better than the MinMin algorithm.

All results are strongly correlated and the trendline through the performance graph has a very high R-squared value – representing a perfect fit.
We conclude that the group method enhances the performance of multicore systems. We also conclude that the group method directly improves performance of multicore systems as the number of cores increases.

Future Thoughts

This research enhances the scheduling of Grid jobs using a novel independent machine and job grouping method and multischeduling. Load balancing was ensured between groups using the proportion of total processing power of machines in the group.

The experiment was executed with a sequential (MinMin) scheduling algorithm. The algorithm was found to be scalable on the multicore systems but scheduling was greatly improved using the group method. In the future, the work can be extended to parallel scheduling algorithms.

This experiment targets the Grid and also uses data from the grid workload archive, giving the close relationship between grid computing and cloud computing, in the future, we hope to adapt the work for the cloud.

The result cannot be standardized because the experiment was executed on systems with different features and family of processors, to standardize the result, the experiment should be executed on a set of systems from the same family of CPU that shares the same features.

Based on the linearity of performance improvement with increasing groups through the computing platforms, we intend to explore further the number of groups used and extrapolate the limit to be able to proffer other solutions.

From the result and analysis, we intend to carry out a performance measure of the three systems by keeping some parameters constant while varying the machine. This will give an idea of the performance measure between the three systems.

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